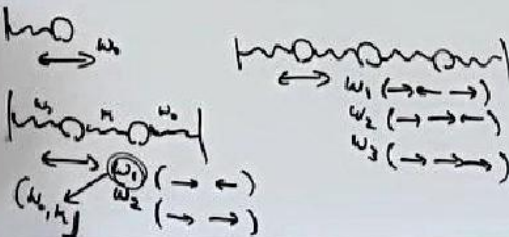
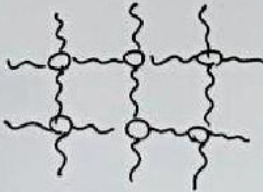




Lecture4 Field quantization and HBT experiment

①

- quantum coherence
- HBT experiment (intensity interferometer)



②

$$\begin{aligned}\nabla \cdot \vec{E} &= \rho \\ \nabla \times \vec{E} &= -\frac{\partial \vec{B}}{\partial t} \\ \nabla \cdot \vec{B} &= 0 \\ \nabla \times \vec{B} &= \mu_0 \vec{J} + \mu_0 \epsilon_0 \frac{\partial \vec{E}}{\partial t}\end{aligned}$$

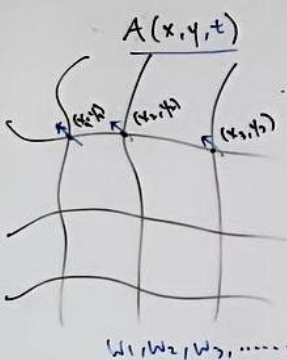
electric

$$\vec{E} = -\frac{\partial \vec{A}}{\partial t}$$

devector magnetic

$$\vec{B} = \nabla \times \vec{A}$$

magnetic



(3)

particle
quantization

$\left. \begin{matrix} x \rightarrow \hat{x} \\ p \rightarrow \hat{p} \end{matrix} \right\} \begin{matrix} 1. \text{ dynamical variables} \rightarrow \text{operators.} \\ 2. \text{ ballistic motion} \rightarrow \text{probability wave} \end{matrix}$
 (Wave function / State)
 probability amplitude

$V(x) + m \frac{d^2 x}{dt^2} = F$ (Newton's equation)

$E = H = \frac{p^2}{2m} + V(x) \rightarrow \hat{H} = \frac{\hat{p}^2}{2m} + V(x)$

$\begin{cases} \frac{\partial H}{\partial x} = \\ \frac{\partial H}{\partial p} = \end{cases} \rightarrow \hat{H} \psi = i\hbar \frac{\partial}{\partial x} \psi$ (Schrödinger's equation)

Maxwell's equation

① $\hat{H} = \hat{E}^2 + \hat{B}^2 = \hat{A}^2$
 ② $|\psi\rangle$ State

quantum particle oscillator

$\hat{H} = \frac{1}{2} m \omega^2 \hat{x}^2 + \frac{\hat{p}^2}{2m} = \hbar \omega \left(\hat{a}^\dagger \hat{a} + \frac{1}{2} \right)$

$\begin{cases} \hat{a} = \hat{x} + i\hat{p} \\ \hat{a}^\dagger = \hat{x} - i\hat{p} \end{cases}$

$\hat{A} = \left(\frac{\hbar}{2m\omega} \right)^{1/2} \hat{a}$
 $\hat{A}^\dagger = \left(\frac{\hbar}{2m\omega} \right)^{1/2} \hat{a}^\dagger$

$\hat{a} = \hat{q} + i\hat{p}$
 $\hat{a}^\dagger = \hat{q} - i\hat{p}$

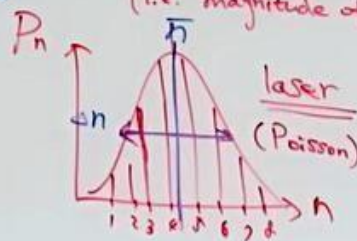
$\hat{A} = \frac{1}{2} \left(\hat{a}^2 + \hat{a}^{\dagger 2} \right)$
 $= \hbar \omega \left(\hat{a}^\dagger \hat{a} + \frac{1}{2} \right)$



photon = a fundamental unit of excitation
(discrete excitation)
for the collective motion of the

Remark ① Single-mode photon is not localized.

electromagnetic field
(i.e. quantized magnitude of field oscillation)



$$|\alpha\rangle = \sum_{\alpha} \frac{1}{\sqrt{N}} |\alpha\rangle$$

(6) $\hat{L}^2 = \hat{L}_x^2 + \hat{L}_y^2 = \hat{L}^2$

$$\hat{A} = \left(\frac{\hbar}{2m\omega} \right)^{1/2} \left(\hat{a} e^{i(\vec{k} \cdot \vec{r} - \omega t)} + \hat{a}^\dagger e^{-i(\vec{k} \cdot \vec{r} - \omega t)} \right) \hat{e}$$

$$\hat{E} = i \left(\frac{k \omega}{2 \epsilon_0 V} \right)^{1/2} \left(\hat{a} e^{i(\mathbf{k} \cdot \mathbf{r} - \omega t)} - \hat{a}^\dagger e^{-i(\mathbf{k} \cdot \mathbf{r} - \omega t)} \right) \hat{e}$$

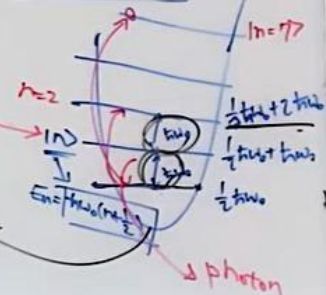
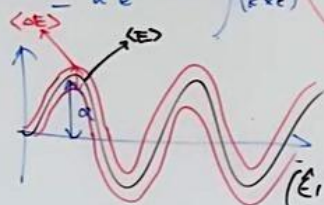
$$\vec{B} = \frac{i}{c} \left(\frac{\hbar \omega}{2\epsilon_0 \omega} \right)^{1/2} \left(\hat{a} e^{i(\vec{k} \cdot \vec{r} - \omega t)} - \hat{a}^\dagger e^{-i(\vec{k} \cdot \vec{r} - \omega t)} \right) (\vec{k} \times \vec{z})$$

$$\langle \hat{E} \rangle = \langle \chi | \hat{E} | \chi \rangle$$

$$\langle \hat{B} \rangle = \langle 4 | \hat{B} | 4 \rangle$$

$$\hat{A} = \left(\frac{1}{2} \right) \hat{A} e^{i\omega t}$$

$$\hat{H}|\psi\rangle = E|\psi\rangle = i\hbar \frac{\partial |\psi\rangle}{\partial t}$$





(5)

photon = a fundamental unit of excitation (discrete excitation) for the collective motion of the mode

Remark ① single-mode photon is not localized pure energy

quantum \rightarrow particle aspect manifestation

interferometric measurement cannot distinguish between different photon distributions $\{ |n\rangle \}$

P_n

electromagnetic field (i.e. quantized magnitude of field oscillation)

laser (Poisson)

$|\alpha\rangle = \sum \frac{\alpha^n}{\sqrt{n!}} |n\rangle$

photon statistic \rightarrow characterize quantum superposition of the electromagnetic field

(1)

$i \rightarrow -i$ complex conjugate

$g^{(1)} = \langle \psi | \hat{E}^{\dagger} \hat{E} | \psi \rangle$

$g^{(2)} = \langle \psi | \hat{E}^{\dagger} \hat{E}^{\dagger} \hat{E} \hat{E} | \psi \rangle$

optical coherence

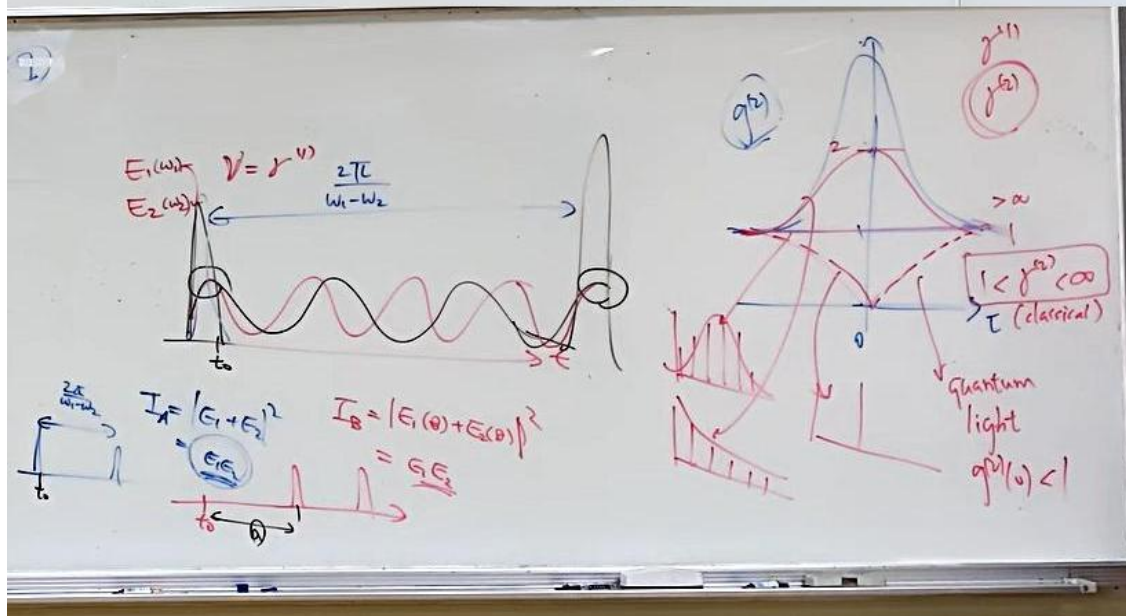
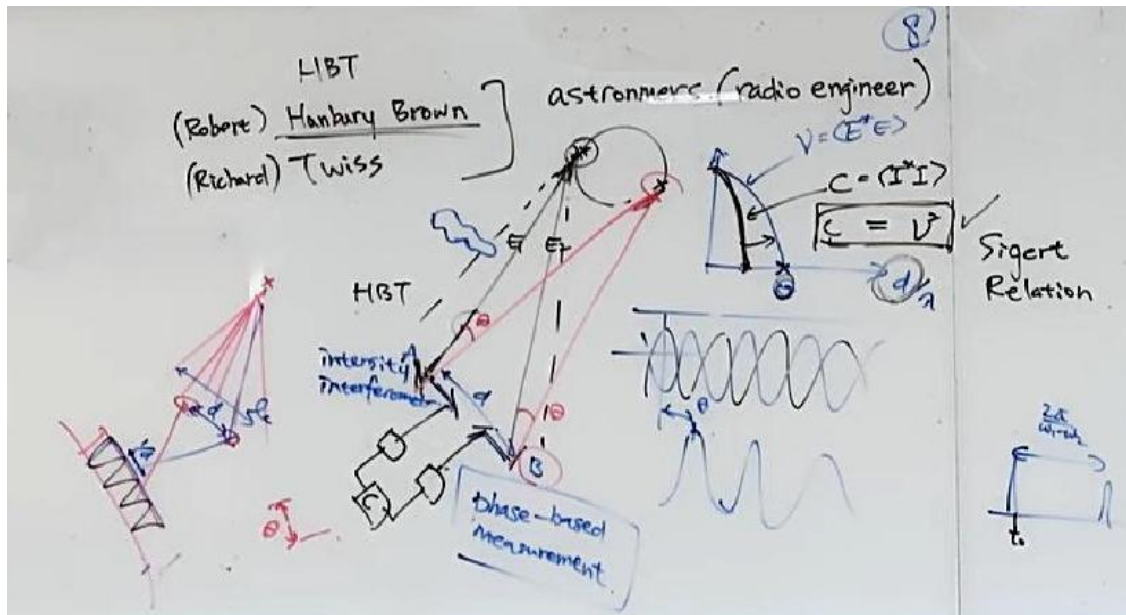
quantum coherence for light

(quantum coherence for particle)

$\hat{n} = \hat{a}^{\dagger} \hat{a}$

$\hat{n} = \hat{a}^{\dagger} \hat{a}$







- ✓ - quantum coherence
- HBT experiment
(intensity interferometer)

